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Internal Improvement.

DESCRIPTION OF THE LIVERPOOL AND MANCHESTER RAILWAY.

There is so little in scenery that is inter-
esting on the turnpike road from Liverpool
to Manchester, that a formal description of
the way between the two towns may ap-
pear to be rather an unpromising undertak-
ing. The traveller along the Railway, how-
ever, will speedily admit that there is little
similitude between the two routes; the whole
character, structure, and appearance of the
Railway being altogether different from the
general aspect of the turnpike road. Instead
of a uniform, flat, and uninteresting country,
the line of Railway is diversified continually
by hill and dale, offered to the contempla-
tion of the traveller in a sort of inverse pre-
sentment, the passenger by this new line of
route having to traverse the deepest recesses,
where the natural surface of the ground is
the highest, and being mounted on the loft-
iest ridges and highest embankments, rid-
ing above the tops of the trees, and over-
looking the surrounding country, where the
natural surface of the ground is the lowest,—
this peculiarity and this variety being occa-
sioned by that essential requisite in a well-
constructed Railway—a levied line—imposing
the necessity of cutting through the high
lands and embanking across the low; thus,
in effect, presenting to the traveller all the
variety of mountain and ravine in pleasing
succession, whilst in reality he is moving al-
most on a level plane, and while the natural
face of the country scarcely exhibits even
those slight undulations which are necessary
to relieve it from tameness and insipidity.

To accomplish a complete survey of the
Railway, we should commence our journey
of observation at the Liverpool end, in the
Company's yard at Wapping. Here the lower
entrance of the great Tunnel is accessible
through an open cutting, 22 feet deep
and 46 wide, being space for four lines of
Railway, with pillars between the lines to
support the beams and flooring of the Com-
pany's warehouses, which are thrown across
this excavation, and under which the wagons
pass to be loaded or discharged through
hatchways or trap doors communicating
with the stores above; wagons loaded with
coal or lime passing underneath the ware-
houses to the open wharves at the Whap-
ping end of the station.

Proceeding along the Tunnel, the line of
Railway curves to the right, or south-east,
till it reaches the bottom of the inclined plane
which is a perfectly straight line, 1980 yards
in length, with a uniform rise of three-
quarters of an inch to a yard. The Railway
from Wapping to the commencement of the in-
clined plane is level; the whole rise, there-
fore, from Wapping to the Tunnel mouth at
Edge-hill, is 123 feet. The Tunnel is 22
feet wide and 16 feet high, the sides being
perpendicular for five feet in height, sur-
mounted by a semicircular arch of 11 feet
radius; the total length is 2260 yards. It is
cut through various strata of red rock, blue
shale and clay, but principally through rock
of every degree of hardness, from the softest
sandstone to the most compact free-stone,
which the axe or the chisel will with diffi-
culty penetrate. It frequently was found
necessary, in the progress of the work, to
make an artificial vault of masonry, which
has been effected by brick arch-work in those
places where the natural rock could not be
trusted to support the superincumbent mass.
The height from the roof of the Tunnel up-
wards to the open surface of the ground, varies
from 5 feet to 70, the greatest mass of
superstratum being in the vicinity of Hope
street and Crabtree-lane. The whole length
of this vast cavern is now furnished with
gas-lights, and the sides and roof are white-
washed, to give better effect to the illumina-
tion. The different colours and peculiar
appearance of the varying strata through
which the Tunnel passes are thus hidden
from view, and the attention is no longer at-
tracted to those faults or slips in the solid
rock which indicate that the whole mass has
been rent asunder by one or more of those
terrible convulsions of nature, of which the
traces are so frequently visible, but of which
no further record remains. The geologist
will be disappointed, in traversing the sub-
terranean vault, to find the natural varieties
converted by lime-water into one uniform
and artificial appearance; but the principle
of utility is paramount in a commercial un-
dertaking.

At the upper or eastern end of the Tun-
nel, the traveller emerges into a spacious and
able area, 40 feet below the surface of the
ground, cut out of the solid rock, and sur-
mounted on every side by walls and battel-
ments. From this area there returns a small
tunnel, 290 yards in length, 15 feet wide,
and 12 feet high, parallel with the large one,
but inclining upwards in the opposite direc-
tion, and terminating in the Company's pre-
mises in Crown street, at the upper and eas-

tern boundary of Liverpool; being the prin-
cipal station for the Railway coaches, and
the depot for coals for the supply of the
higher districts of the town.

Proceeding eastward from the two Tun-
nels, the road passes through a Moorish
archway, at present unfinished, which is to
connect the two Engine-houses, and will
form the grand entrance to the Liverpool
station. The structure is from a spirited
design of Mr. Foster's. The traveller now
finds himself on the open road to Manches-
ter, and has an opportunity of contemplating
the peculiar features of a well-constructed
Railway, the line in this place being per-
fectly level; the slight curve which was un-
avoidable, beautifully set out; the road-way
clean, dry, and free from obstructions; and
the rails firmly fixed on massive blocks of
stone. Crossing Wavertree lane, the Rail-
way descends for 54 miles at the rate of four
feet in the mile, a declivity so slight and uni-
form as not to be perceived by the eye, but
still sufficient to give a mechanical advantage
and facility of motion to a load passing in
that direction. The road a fute beyond Wav-
ertree lane is carried through a deep marle
cutting, under several massive stone arch-
ways, thrown across the excavation to form
the requisite communications between the
roads and farms on the opposite sides of
the Railway. Beyond the marle cutting is
the great rock excavation through Olive
Mount, about half a mile to the north of the
village of Wavertree. Here the traveller
passes through a deep and narrow ravine,
70 feet below the surface of the ground, lit-
tle more space being opened out than suffi-
cient for two trains of carriages to pass each
other; and the road winding gently round
towards the south-east, the prospect is bound-
ed by the perpendicular rock on either
side, with the blue vault above, relieved at
intervals by a bridge high over head, con-
necting the opposite precipices. The sides
of the rock exhibit already the green surface
of vegetation, and present altogether far
more of the picturesque in their appearance
than might be expected from so recent an
excavation. At night, when the natural
gloom of the place is farther deepened, the
scene from the bridges above will readily be
imagined to be novel and striking. The light
of the moon illuminating about half the
depth, and casting a darker shade on the
area below—the general silence interrupted
at intervals by a noise like distant thunder
—presently a train of carriages led on by
an Engine of fire and steam, with her lamps
like two furnaces; throwing their light on-
ward in dazzling signal of their approach—
with the strength and speed of a war-horse
the Engine moves forward with its glorious
cavalcade of merchandise from all countries
and passengers of all nations. But the spec-
tacle is transient as striking; in a moment
the pageant is gone—the meteor is passed,
the flaring of the lamps is only seen in the
distance, and the observer, looking down
from the battlement above, perceives that
all again is still, and dark, and solitary.

Emerging from the Olive Mount cutting,
you approach the great Roby embankment,
formed of the materials dug out of the excava-
tion we have described. This embank-
ment stretches across the valley for about
two miles, varying in height from 15 to 45
feet, and in breadth at the base from 60 to
135 feet. Here the traveller finds himself
affected by sensations the very reverse of
what he felt a few minutes before. Mounted
above the tops of the trees, he looks around
him over a wide expanse of country, in the
full enjoyment of the fresh breeze, from
whatever quarter it may blow.

This vast embankment strikingly exhibits
how much may be accomplished when our
efforts are concentrated on one grand object.
There is a feeling of satisfaction by no means
common-place, in thus overcoming obsta-
cles and surmounting difficulties, in making
the high places low and the rough places
plain, and advancing in one straight and di-
rect course to the end in view; while the
pleasure afforded by the contemplation of
this great work is farther enhanced, when
considered in contrast with ordinary and ev-
ery-day impressions.

After passing the Roby embankment, you
cross the Huyton turnpike road, leaving
Huyton Church and village on the left hand,
and proceed in a slightly curved direction to
the bottom of the inclined plane at Whiston,
between seven and eight miles from the
Company's station in Liverpool. This plane
rises in the ratio of three-eighths of an inch
in a yard, or 1 in 96. It is a mile and a half
long in one straight line, and the inclination
(being so slight) would scarcely attract ob-
servation, did not a decrease in the speed of
the carriage indicate that an important
change had taken place in the level of the
way. At the top of the Whiston inclined
plane there is a portion of the road (nearly
two miles in length) on the exact level.—
About half a mile from the top of the in-
clined plane, the turnpike road from Liver-
pool to Manchester crosses the line of the Rail-
way at an acute angle of 34 degrees, and is
carried over the Railway by a substantial
stone bridge, of very curious and beautiful
construction, being built on the diagonal or
skew principle, each stone being cut to a
particular angle to fit into a particular place,
the span of the arch, measured at the face,
being 54 feet, while the width of the Rail-
way underneath, measured from wall to wall,
is only 80 feet—each face of the arch ex-

tending diagonally 45 ft. beyond the square.
Rainhill bridge is nine miles from the Com-
pany's yard in Wapping, and it was under-
neath and on each of this bridge that the
experiments took place with the Locomotive
Engines which contended for the premium
of £500 in October 1829.

Passing over the summit level at Rainhill,
we come to the Sutton-inclined plane, which
descends in the opposite direction, and is sim-
ilar in extent and inclination to the Whis-
ton plane, the top level being 82 feet above
the base of each plane. Par Moss is the
next object of attention, the road way across
the principal part of it being formed by the
deposits of heavy material (clay and sand)
dug out of the Sutton inclined plane. This
Moss is about 20 feet deep, and the material
forming the Railway, as it was deposited,
sank to the bottom, and now forms an em-
bankment in reality 26 feet high, tho' only
four or five feet appears above the surface
of the Moss. The borders of this waste are
in a state of increasing cultivation, and the
carrying of the Railway across this Moss
will hasten the enclosure of the whole area.

Leaving Par Moss, we soon approach the
great valley of the Sankey (about half way
between Liverpool and Manchester, with its
Canal at the bottom, and its flats or barges
in full sail passing to and fro, between the
River Mersey, near Warrington, and the
great Canal districts near St. Helen's.—Over
this valley and Canal, and over the topmasts
and high peaks of the barges, the Railway
is carried along a magnificent viaduct of
nine arches, each 50 feet span, built prin-
cipally of brick, with stone facings, the height
from the top of the parapets to the water in
the Canal being 70 feet, and the width of
the Railway between the parapets 25 feet.
The approach to this great structure is along
a stupendous embankment, formed prin-
cipally of clay, dug out from the high lands
on the borders of the valley. Looking over
the battlements, there is a fine view down
the valley to the south—Warrick spire ris-
ing in the distance, and below you, the lit-
tle stream of the Sankey running parallel
with the Canal; whilst the masts and sails
of the vessels, seen at intervals in the land-
scape is no longer visible, present a vivid
specimen of inland navigation. Immediately
below you, the barges, as they approach the
bridge, escape from view for a few minutes,
till, having sailed under your feet, they be-
come again visible on the opposite side of
the viaduct.

On leaving the Sankey, we speedily ap-
proach the town of Newton, or rather the
borough; for this ancient and loyal place
sends two representatives to Parliament, un-
der the auspices of Colonel Legh, M. P. A
few hundred yards to the south of the town
the Railway crosses a narrow valley by a
short but lofty embankment, and a hand-
some bridge of four arches, each 40 feet
span. Under the eastern arch of the tur-
npike road passes from Newton to Warring-
ton, and beneath another arch flows a stream
which turns an old corn mill, immediately
below the bridge. Adjacent also, is situ-
ated one of those antique mansions, built in
the ancient baronial styles, whose white ex-
terior, with black oak crossings, and pointed
gables, harmonizes well with the rude sce-
nery around.

A few miles beyond Newton is the great
Kenyon excavation, from which about 800,
000 cubic yards of clay and sand have been
dug out, part being carried to form the
line of embankment to the east and west of
the cutting, and the remainder, deposited as
spoil banks, may be heaped up, like Pliocene
upon Ossa, towering over the adjacent land.
Near the end of this cutting, the Kenyon and
Leigh Junction Railway joins the Liverpool
and Manchester line by two branches, point-
ing to the two respectively. This Railway
joins the Bolton and Leigh line, and thus
forms the connecting link between Bolton,
Liverpool, and Manchester. From the
Kenyon excavations the transition is easy to
the Broseley embankment, formed of the
material dug out of the cutting, as before
described. Moving onward, we pass over
Bury lane and the small River Gless, or
Glazebrook, being arrived in the borders of
the Chat-Moss. This barren waste compre-
sides an area of about twelve square miles,
varying in depth from 10 to 26 feet, the
whole mass being of so spongy and soft a
texture that cattle cannot walk over it. The
bottom is composed of clay and sand, and it
is not an uninteresting, if not a very profit-
able speculation, to carry our ideas back to
that remote period when the sea flowed
over the basin of this huge fungus. There
are they who profess, by examining the ve-
getable fibre of the Moss, to calculate its
age; as the fortune-teller will cast your na-
tivity by the furrows in your hand. No
doubt this vegetable matter is still increas-
ing. The flower and the leaf of the heather
still bud, grow to maturity, and fall; and
the process of decomposition amalgamates the
new and the old fibre; but what is thus de-
posited has been previously extracted from
the Moss, save what has been supplied from
the hydrogen and other gases absorbed and
combined in this great laboratory. At a very
moderate calculation Chat Moss comprises
sixty millions of tons of vegetable matter;
and we shall leave to philosophers to calcu-
late in how many centuries this weight could
be drawn from the clouds and the air.—
Northward of the Moss, in the distance, is
Tildesley Church, one of the modern Parlia-

mentary edifices! and as we approach the
eastern boundary, conspicuous on a gentle
eminence to the left, is Worsley Hall, the
seat of R. H. Bradshaw, Esq. M. P. so well
known as Trustee for the Duke of Bridge-
water's Canal.

Beyond Chat Moss we traverse the Bar-
ton embankment, crossing the low lands for
about a mile between the Moss and the
Worsley Canal, over which the Railway is
carried by a neat stone bridge. At this spot
it is evident you are approaching a manu-
facturing district. On the banks of the Can-
al a great cotton factory rears its tall sides,
with its hundred windows, and the fly-wheel
of its steam engine pursuing its continuous
and uniform revolutions, as if symbolical of
that eternal round of labour and care, of abun-
dant toil and scanty remuneration, of
strained exertion and insufficient repose,
which, through day and night, through sea-
son and harvest, through years of civiliza-
tion and ages of barbarism, have been the
condition and tenure on which the existence
of so large a portion of mankind has de-
pended.

From the Barton embankment we soon
arrive at Eccles, four miles from Manches-
ter, leaving to the right the vicarage and pa-
rish church of that village. Between this
place and Manchester the Railway passes at
no great distance from several country seats
and villas, whose rich lawns and flourishing
plantations afford an agreeable variety, al-
ter the great sand hills at Kenyon or the
wide waste of Chat Moss.

The immediate approach to Manchester,
by the Railway, is through a portion of Sal-
ford, as little interesting as can well be im-
agined. Over the River Irwell the Railway
is carried by a very handsome stone bridge,
and then over a series of arches, into the
Company's station in Water street and Li-
verpool road, Manchester; from which the
traveller whose object is pleasure rather than
business, will probably make his way, with-
out loss of time, to the more genial attrac-
tions of the Albion Hotel, or New Bridgewater
Arms.—Booth's R. R. Report.

Mathematics.

Solution to quest. XXXIII. by Ned Numscull. Let
ABC represent the horizontal plane; B the point where
the wheel touches it; DHE a diameter perpendicular
to the plane, and EFH parallel to it. Let the radi-
us = H be taken to express the weight of the barrow and
the direction in which the axis are to be elevated, and
resolve it into perpendicular forces GI, IH. Now GI
is the only part of the force GH which is employed in
pushing the barrow horizontally, and is the same as
though it were collected at the point I and employed in
turning the wheel round; but this effect is, by me-
chanics = GI.IH = a max; by hypothesis, it is well known
that GI = IH and the angle of elevation = 45 degrees.

Solution to quest. XXXIV. by Moses Ebbow. It is
well known that if the two sides of a triangle represent
the quantities and directions of two forces, the base will
represent a force equivalent to both; therefore there are
given two sides of a plane triangle and an angle oppo-
site to one of them to determine the other side, a ques-
tion which I would recommend to the notice of the
Sophists.

A general solution by Zero. Let P, S and Q
represent the forces, A the angle which P make with S, and
x the angle the same force makes with Q; then, art. 24,
Venturoli's Mechanics, S squared = P squared + 2P.Q.
cos. x + Q squared, and
sin A = $\frac{Q}{S}$ sin x;
hence S squared = $\frac{Q \cos A}{\sin A}$ squared

= $\frac{P \sin A \text{ squared} + Q \cos A \text{ squared}}{\sin A \text{ squared}}$, from which by
an obvious reduction cos x = $\frac{P \sin A \text{ squared} - Q \cos A \text{ squared}}{2PQ}$

Cor. I. If $\cos x = 1$; then $\cos A = \frac{Q \cos A \text{ squared} - P \sin A \text{ squared}}{2PQ}$
cos A squared = cos 2A; $\therefore x = 2A$, and $S = 2P \cos A$.

II. If $\cos x = 0$; then $\cos A = \frac{P \sin A}{S}$
Solution to quest. XXXVIII. by Digory Sweep-
stakes. Since CT is parallel to HF, $\angle HFC = \angle FCF$
and arc HC = arc FT. Because AZ = ZB (4.1), ZN
= ZC (24.4), $\angle AZB$ is bisected (2cor. 4.3) $\therefore \angle NZH$
= $\angle HZC$ (13.1) and the arc NH = HC. Again, be-
cause the arc AF = arc FB (4.3), CF bisects the ver-
tical angle ACB, but by construction CG = CB, be-
cause it is the supplement of $\angle C$; \therefore arc HC = AM =
NH = AF = FT. Q. E. D.

Solution to same by Uncle Ben. In the triangle
AB, since the diameter HF is drawn at right angles
to AB, it bisects it (4.3) $\therefore AZ = ZB$ and $\angle AZE = \angle$
 $\angle BZE$. But $\angle NZC = \angle ZC$ when $AZ = ZB$ (24.4), hence
NC is bisected at right angles, and NH = HC (4.3).
Also the alternate angles FCI and CFH being equal
the arcs which they subtend are equal (6.3).
Again, the triangles MGA and BGC are similar (6.4)
for the vertical angles MGA and BGC are equal, and
the sides about the equal angles are proportional (24.4)
 $\therefore MA \text{ : } GC = NA \text{ : } CB$; but (2cor. 4.3) the angles at
V are right angles as well as HCF (8.3) \therefore HC and
MB are parallel (4.2) and $\angle CGB = \angle CAM$, con-
sequently in the triangles AHC, the side AC
is common, $\angle CAM = \angle ACH$, and $\angle CMA = \angle AHC$, they
are therefore equilateral (7.2) \therefore HC = MA and the
arcs which they subtend are equal (3.3). Q. E. D.

This is a very ingenious solution, and we hope our
correspondent will try his skill on the subsequent propo-
sitions.

Cor. I. by Zero. CD is perpendicular to HF.
II. The arc MH = CB. For AH = HB and AM
= HC

III. The $\angle ACH =$ half the supplement of the
vertical angle ACB.

IV. If R be the centre of the circumscribing circle,
then the angle CZB = CRB. For ZA = ZB, \therefore CZB
= 2ZAB (6.2) = RB (5.3). Hence a circle will pass
through the points C, Z, R, B, (cor. 6.3).

Quest. XLIX. A person rows from A to B 10 miles
and back again from B to A in five hours, the tide flow-
ing uniformly in the same direction the whole time; and
he finds that he can row 8 miles with the tide in the
same time that he can row 3 miles against it. Required
the velocity of the tide supposing it to communicate
or destroy a velocity equal to its own?

Quest. L. by Zero. The whole surface of a right
cylinder is six times the area of the base. Required
the ratio of the diameter to the diameter of the base.

Quest. LI. by Zero. Four agents A, B, C and D can
jointly produce a given effect in 10 hours. A's agency
alone would produce it in 26 hours, but with the assis-
tance of E the difficulty can be surmounted in the same
time that it would take B, C and D together; B can ac-
complish the same object as soon as C and D united,

and A and D in the same time as B and E: How long
will it take for their joint and separate production of
this effect?

Quest. LII. Prop. 7. The rectangle ED, EH is
equal to the sum of the sides, OC.
We had prepared the above when we received a com-
munication from "Madiah Gandersbank containing solu-
tion to questions 38 and 39. They are concisely and
perspicuously demonstrated and shall appear in our next.

Continuation of our article on SOUND.

Let us now examine how the air is modified in dif-
ferent parts of the wave; and, for this purpose, let us
imagine planes parallel to the piston, which divide the
column of air into lamina, or thin slices, such as *abcd*,
cdef, &c. having all the same thickness; it is probable
that in each lamina all the molecules of air from the
axis to the centre of the tube, undergo the same modifi-
cations, for all are similarly circumstanced. There-
fore, to understand what has happened to the whole
mass of air which composes the wave, it is sufficient to
know what has happened to a molecule of each lamina.
Now since the air which was included within Pp and
AA has been compressed in its totality, and reduced so
as to occupy only the space SsAA, it necessarily fol-
lows that the molecules in each lamina have experi-
enced two effects; 1st, they have become compressed; 2d,
they have received a certain impulsive celerity, i. e. a
celerity which removes them from the centre of the
shock or of the piston which moved them.

It is evident that, in the whole length of the wave,
the different lamina cannot be in the same state: the
last lamina, for example, that which touches AA, has
only received a very small velocity and a very slight
compression, because the motion has only just reached
there; the first lamina, that which touched Ss, has al-
ready regained its state of rest, since we are consid-
ering the phenomena at the instant in which the
piston was stopped; and as the lamina has no longer
any velocity, it has for that reason no compression; it
has already communicated all it possessed, on the
contrary, the lamina which are towards the middle of
the wave have at the same time the greatest compres-
sion and the most celerity. There is therefore a certain
order in the various modifications of the different lam-
inae, both as respects the velocity of the molecules of
the air and their compression. This order depends on the
increasing and decreasing velocities through which the
piston passed in being transferred from Pp to Ss.

We can represent, by a figure which addresses the
eye, all the motions which characterize a wave from its
origin to its termination; for this purpose, it is sufficient
to erect on the line SA, which expresses its length,
perpendiculars which represent the degree of compres-
sion of the corresponding lamina; the extremities of
these perpendiculars will form a line whose curvature or
sinuosities will accurately represent the order in
which the compressions of the successive laminae suc-
ceed one another. At S the height of the perpendicu-
lar will be nothing because the compression is nothing,
it will be the same at A; at X the height of the perpen-
dicular will be for example, XX, at Y it will be YY,
at M it will be MM, &c. so that the curve of com-
pressions SMA might be a semi-circumference of a circle.
But we perceive that, on this length SA, we can trace
a multitude of continuous curves passing through the
points S and A, and even one of these curves being
given, we can always give the piston such a motion in
its passage from Pp to Ss that it may excite a wave
whose successive compressions should be represented
by this curve. When there are many sinuosities in the
curve of compressions we say that the corresponding
undulation is an *indented wave*.

After having analysed the various modifications which
the piston may impress on the column of air whilst
passing from Pp to Ss in the interval of one second,
we may endeavor to ascertain what will take place in
the succeeding intervals, the piston always continuing
to stop at Ss. The air momentarily compressed from Ss
to AA cannot remain in this state; for the tube being open
at A, it follows that after a certain time, the excess of
air must egress, and the whole column return to a state
of rest. Now, it is demonstrated, in mechanics, that
compression and velocity are communicated successively
in the following manner: in the first instant of the
second second the velocity passes to the right of AA,
invades a first lamina, and at the same time the lamina
which touches the piston returns to a state of rest; in
the second instant a second lamina on the right of AA
is invaded, and a second lamina in front of the piston
sinks to rest; in the third instant the motion reaches
the 3d lamina in front of AA, and a state of rest reaches
the third lamina in advance of the piston, &c.; so that
at the end of the second second, the air is in a state of
rest from S to A, and is in a state of agitation from A
to B; the length AB is equal to SA, and moreover the
compressions and velocities from A to B are exactly
what they were from S to A. Thus, the undulation
advances and is conveyed, in some measure uniformly,
by preserving its length and all its characters; at the
end of the third second it would be at BC; at the end
of the fourth, at CD, &c.

The wave which we have just described, in which
all its lamina are compressed and all the velocities im-
pulsive is called a *condensed wave*, or sometimes *condens-
ing wave*.

But it is easy to see that the inverse phenomena are
developing at the left of the piston Pp whilst it is
transferred to Ss. In fact, a greater space has
been presented to the column of air, the first lamina
rushes after the piston by being rarified, the second
rushes after the first and takes its place, &c. &c.; and
after the first second, when the piston stops at Ss the
rarefaction is perceived as far as a. The wave which
results from it is called a *rarified wave*, or rather *vari-
fying wave*; its length is exactly the same as that of the
condensed wave which is produced before the piston,
the rarefactions are nothing at Ss and at aa, and, in all
the lamina, the velocities are *appulsive*, i. e. directed to-
wards the centre of the shock.

The rarified wave is also propagated, successively,
through the whole extent of the column of air, preserv-
ing every where the same length and the same succe-
sion of velocities and rarefactions.

These considerations shew us, now, the principles on
which the phenomenon of hearing rests, for if we imag-